

TITLE OF THE INVENTION
COMPUTER-GENERATED HOLOGRAM

BACKGROUND OF THE INVENTION

5 The present invention relates generally to a computer-generated hologram, and more particularly to a computer-generated hologram that is relatively simple to fabricate and serves well to reconstruct a three-dimensional image of high quality at high resolution.

10 Holography has been developed as one of long-standing desires to record three-dimensional images on planes. Holography is a sort of technology for recording 3D image of an object making use of a laser light source of high coherence, and a 3D image display medium
15 fabricated by holography is called a hologram. Holograms have such difficulties that they can never be fabricated unless the object to be recorded is substantially present, because they are actually produced by a process wherein laser light is directed to the object for recording its
20 image in a photosensitive material. In addition, the object must be kept still at the wavelength level of light during recording, and so it is difficult to record objects often in motion such as flexible objects and figures. On the other hand, there is a stereogram that makes a number
25 of two-dimensional images created by still cameras, video cameras, computer graphics (CG), etc. stereoscopically visible. The stereogram, by definition, is a medium that makes it possible for a viewer to see an image that varies

with viewing directions. Given a parallax image of an object viewed from a plurality of directions, three-dimensional effects are obtainable because the image of the object can be seen depending on viewing directions.

5 Now widely used is a stereogram obtained with a lens array such as a lenticular or fly's eye lens located on a printing medium. The stereogram may also be fabricated by means of holography, and is called a holographic stereogram. The holographic stereogram developed to date
10 is roughly broken down to two types, one called a two-step holographic stereogram and the other a one-step holographic stereogram after the number of recording photosteps.

 The two-step holographic stereogram, true to its
15 name, is fabricated by a two-photostep process, whose details are set forth in Patent Publication 1. Briefly speaking, the two-photostep process comprises three steps, i.e., a step (1) of providing two-dimensional images of the object to be recorded, which are viewed from a number
20 of positions spaced away from it, a photostep (2) of dividing a first photosensitive material into a number of areas, wherein an image corresponding to a specific area of the areas provided in step (1) is holographically recorded in that area thereby preparing a first hologram,
25 and a photostep (3) of directing reconstructing illumination light to the first hologram so that the reconstructed image is recorded in a second photosensitive material to prepare a second hologram. On the other hand,

the one-step holographic stereogram, as its name implies,
is fabricated by a one-photostep process, whose details
are set forth in Patent Publications 2 and 3. Briefly
speaking, this process comprises a step (1) of finding
5 light rays to be radiated from a number of positions on a
photosensitive material, and a photostep (2) of dividing
the photosensitive material into a number of areas,
wherein the light ray to be reconstructed from a specific
area of the areas found in step (1) is recorded in that
10 specific area.

Whether the two-step holographic stereogram or the
one-step holographic stereogram makes it possible for the
viewer to see a three-dimensional image, and so is now
used as a general-purpose medium for the reconstruction of
15 3D images.

For the hologram that can reconstruct 3D images,
there is also known a 3D image reconstructing computer-
generated hologram (CGH) proposed by the inventors (see
Patent Publications 4, 5, 6 and 7). In this CGH, the
20 surface of the object is replaced by a set of point or
line light sources for calculation of phases and
amplitudes on the hologram plane.

For the CGH obtained by the process wherein the
surface of the object is replaced by a set of point or
25 line light sources, it is also proposed to reproduce
images in color upon reconstruction by white light, as set
forth in Patent Publication 8.

Patent Publication 1

JP-A 52-4855

Patent Publication 2

Patent No. 2,884,646

Patent Publication 3

5 JP-A 6-266274

Patent Publication 4

JP-A 9-319290

Patent Publication 5

JP-A 11-202741

10 Patent Publication 6

JP-A 2001-13858

Patent Publication 7

JP-A 2001-13859

Patent Publication 8

15 JP-A 2000-214751

Patent Publication 9

JP-A 2002-72837

Non-Patent Publication 1

20 Junpei Tsuji, "Selection of Physics, Holography",
published by Shokabo Co., Ltd. (November 5, 1997), pp. 33-
36.

The aforesaid prior art 3D image reconstruction
processes have their own merits and demerits. Print with
a lens array such as a lenticular or fly's eye lens has a
25 merit of dispensing with any holographic photostep relying
upon laser light, but it has several demerits of decreased
resolution and increased thickness due to the need of a
physical pixel structure such as a lens array.

The two-step holographic stereogram comprises a pixel structure-free hologram plane and so has high resolution; however, it has problems in that some holographic photosteps are required with distortion in
5 images.

The one-step holographic stereogram has no image distortion yet with more parallaxes; however, its problems are that the pixel structure is noticeable on the hologram plane and some considerable holographic photosteps result
10 in the need of special image processing.

The three-dimensional image reconstruction CGH proposed by the inventors has several merits of higher resolution, more parallaxes, no image distortion and no need of using any holographic photostep, but there are
15 elusive problems in that some special image processing operations (such as hidden surface removal and correction of luminance) are necessary.

SUMMARY OF THE INVENTION

20 A primary object of the invention is to provide a solution to the demerits of each of the above prior arts by the provision of a computer-generated hologram, which has ever higher resolution, much more parallaxes and no image distortion problem, and which makes any holographic
25 photoset unnecessary and image processing easy.

According to one aspect of the invention, the above object is accomplished by the provision of computer-generated hologram with a complex amplitude of object

light recorded therein so that a stereoscopic object is reconstructible, characterized in that:

a group of virtual point light sources is spatially set on a side opposite to a viewing side of the hologram,
5 a luminance angle distribution $T_{WLCi}(\theta_{xz}, \theta_{yz})$ of divergent light from each virtual point light source in said group of virtual point light sources toward said viewing side is set in such a way as to be equal to a luminance angle distribution on a surface of an object to be recorded as
10 said virtual point light source is viewed from the viewing side, and an initial phase of divergent light diverging from each of said virtual point light sources is kept constant independently among said virtual point light sources, so that divergent light beams from said virtual
15 point light sources are superposed one upon another and recorded as object light in any position on a viewing side of said group of virtual point light sources, on which the divergent light is incident.

In this aspect of the invention, each virtual point
20 light source in said group of virtual point light sources may comprise a one-dimensional point light source that is also a two-dimensional straight line light source.

Preferably in the first aspect of the invention, the
initial phase of the divergent light diverging from each
25 virtual point light source in the virtual point light source group is mutually independently determined, because the amplitude distribution of object waves by the

synthesis of light from all light sources is averaged and so unnecessary noises are substantially removed from a reconstructed image.

According to another aspect of the invention, there
5 is provided a computer-generated hologram with a complex amplitude of object light recorded therein so that a stereoscopic object is reconstructible, characterized in that:


upon incidence of given reconstructing illumination
10 light thereon, there is reconstructed diffraction light that diverges from each point in a spatial group of virtual points toward a viewing side of a hologram wherein said spatial group of virtual points is located on a side opposite to the viewing side, and wherein a luminance
15 angle distribution of light propagating in such a way as to diverge from each virtual point toward the viewing side of the hologram is equal to a luminance angle distribution of light that diverges from a surface of a recorded object to a viewing side thereof via each point in said group of
20 virtual points.

In this aspect of the invention, each virtual point in said group of virtual points may comprise a one-dimensional point that is also two-dimensional straight line.

25 According to yet another aspect of the invention, there is provided a computer-generated hologram with a complex amplitude of object light recorded therein so that a stereoscopic object is reconstructible, characterized in

that:

a group of virtual condensing points is spatially set on a viewing side of a hologram, an luminance angle distribution $T_{WLCi}(\theta_{xz}, \theta_{yz})$ of convergent light incident on
5 each condensing point in said group of virtual condensing points from a side opposite to the viewing side is set in such a way as to be equal to a luminance angle distribution on a surface of an object to be recorded as viewed for the viewing side through said virtual
10 condensing point, and a phase of convergent light incident on each condensing point in said group of virtual condensing points is kept constant independently among said virtual condensing points, so that convergent light beams are superposed one upon another and recorded as
15 object light in any position on a side opposite to a viewing side of said group of virtual condensing points, on which convergent light is incident.

In this aspect of the invention, each virtual condensing point  in said group of virtual condensing points may
20 comprise a one-dimensional condensing point that is also a two-dimensional condensing straight line.

Preferably in the third aspect of the invention, the initial phase of the converging light incident on each virtual condensing point in the virtual condensing point
25 group is mutually independently determined, because the amplitude distribution of object waves by the synthesis of light all condensing points is averaged and so unnecessary

noises are substantially removed from a reconstructed image.

According to the fourth aspect of the invention, there is provided a computer-generated hologram with a
5 complex amplitude of object light recorded therein so that a stereoscopic object is reconstructible, characterized in that:

upon incidence of given reconstructing illumination light thereon, there is reconstructed diffraction light
10 that diverges from each point in a spatial group of virtual points on a viewing side of a hologram, wherein a luminance angle distribution of light diverging from each virtual point is equal to a luminance angle distribution of light diverging from a surface of a recorded object on
15 a viewing side thereof through each point in said group of virtual points.

In this aspect of the invention, each virtual point in said group of virtual points may comprise a one-dimensional point that is also a two-dimensional straight
20 line.

In accordance with the computer-generated hologram of the invention, the position of condensing reconstruction light diffracted from the hologram is separated from the object to be reconstructed and the
25 hologram plane. It is thus possible to achieve a computer-generated hologram that has no pixel structure on the hologram plane with much more parallaxes and ever higher resolution, creating a reconstructed image having

no image distortion problem and much higher quality. It is also possible to provide a computer-generated hologram that makes any holographic photostep unnecessary, ensures simplified image processing, and makes a computer graphic
5 image of a three-dimensional object obtained on commercial software available as the stereoscopic image to be recorded.

Still other objects and advantages of the invention will in part be obvious and will in part be apparent from
10 the specification.

The invention accordingly comprises the features of construction, combinations of elements, and arrangement of parts, which will be exemplified in the construction hereinafter set forth, and the scope of the invention will
15 be indicated in the claims.

BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is illustrative of the principles of the computer-generated hologram according to the invention.

20 Fig. 2 is illustrative of how a stereoscopic image is reconstructed from the computer-generated hologram of Fig. 1.

Fig. 3 is illustrative of how to fabricate the computer-generated hologram of Fig. 1.

25 Fig. 4 is illustrative of another embodiment of the computer-generated hologram according to the invention.

Fig. 5 is illustrative of how a stereoscopic image is reconstructed from the computer-generated hologram of

Fig. 4.

Fig. 6 is illustrative of how to fabricate the computer-generated hologram of Fig. 4.

5 DESCRIPTION OF THE PREFERRED EMBODIMENTS

In accordance with the rudimental principles of the computer-generated hologram of the invention, used to deprive a pixel structure of a hologram plane, at a position spaced away from the hologram plane there are
10 defined a multiplicity of virtual point light sources having a radiance that varies with a radiation direction and is equal to the radiance of an object surface in that direction or a multiplicity of virtual condensing points having a radiance that varies with a condensing direction
15 and is equal to the radiance of an object surface in that direction, so that a computer-generated hologram is fabricated by using light that radiates from those virtual point light sources or condenses onto those virtual condensing points as virtual object light, thereby
20 obtaining a computer-generated hologram (CGH) that has higher resolution and can dispense with any holographic photostep.

The principles of the computer-generated hologram according to the invention are now explained.

25 As shown in Fig. 1 illustrative of the principles of the invention, a group 11 of virtual point light sources, an object 10, a CGH 12 and a viewer M are located in this order along a + direction along a z-axis. With the center

of CGH 12 defining the origin of coordinates, x- and y-axes are determined in mutually orthogonal directions and in a direction orthogonal with respect to the z-axis. With the coordinates of virtual point light source group 5 11 described in terms of (x_1, y_1, z_1) , the coordinates of object 10 in terms of (x_0, y_0, z_0) and the coordinates of CGH 12 in terms of (x_2, y_2, z_2) , the radiance of object 10 in θ_{xz} and θ_{yz} directions at a point S (x_0, y_0, z_0) that is observable from viewer M among the points of intersection 10 of object 10 with a straight line Q_iP_j connecting an i-th virtual point light source $Q_i (x_1, y_1, z_1)$ with a j-th cell $P_j (x_2, y_2, z_2)$ of CGH 12 is represented by $T_{WLCi} (\theta_{xz}, \theta_{yz})$. Here θ_{xz} is an angle of straight light Q_iP_j with the z-axis upon projected onto an x-z plane, and θ_{yz} is an angle of 15 straight line Q_iP_j with the z-axis upon projected onto a y-z plane.

Given that λ_c is a wavelength, A_{WLCi} is the amplitude of wavelength λ_c of virtual point light source Q_i , the initial phase is ϕ_{WLCi} , and r_{ij} is the Q_i to P_j distance. 20 Then, the complex amplitude value $O_{WLC} (x_2, y_2, z_2)$ of an object wave 1 at $P_j (x_2, y_2, z_2)$ becomes

$$O_{WLC} (x_2, y_2, z_2) = \sum_{i=1}^M \{ A_{WLCi} T_{WLCi} (\theta_{xz}, \theta_{yz}) / |r_{ij}| \} \times \exp[j\{(2\pi/\lambda_c) r_{ij} + \phi_{WLCi}\}] \quad \dots (1)$$

Here the incident vector of reference light 2 incident on CGH 12 and consisting of parallel light is

given by (R_x, R_y, R_z) , the amplitude of wavelength λ_c thereof by R_{WLC0} , and the phase thereof at the origin of the coordinates by ϕ_{WLC} . Then, the complex amplitude value of reference light 2 becomes

$$5 \quad R_{WLC}(x_2, y_2, z_2) = R_{WLC0} \cdot \exp[j\{2\pi/\lambda_c\} \times (R_x x_2 + R_y y_2 + R_z z_2) / (R_x^2 + R_y^2 + R_z^2)^{1/2} + \phi_{WLC}\}] \quad \dots (2)$$

The intensity value, $I_{WLC}(x_2, y_2, z_2)$, of interference fringes of object wave 1 and reference light 2 at $P_j(x_2, y_2, z_2)$ is

$$10 \quad I_{WLC}(x_2, y_2, z_2) = |O_{WLC}(x_2, y_2, z_2) + R_{WLC}(x_2, y_2, z_2)|^2 \quad \dots (3)$$

In the above equations, the Q_i to P_j distance r_{ij} is

$$R_{ij} = \{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2\}^{1/2} \quad \dots (4)$$

The angle θ_{xz} of straight line $Q_i P_j$ with the z-axis upon projected onto the x-z plane is

$$15 \quad \theta_{xz} = \tan^{-1}\{(x_2 - x_1)/(z_2 - z_1)\} \quad \dots (5)$$

The angle θ_{yz} of straight line $Q_i P_j$ with the z-axis upon projected onto the y-z plane is

$$\theta_{yz} = \tan^{-1}\{(y_2 - y_1)/(z_2 - z_1)\} \quad \dots (6)$$

The initial phases ϕ_{WLCi} of virtual point light sources Q_i are mutually independently and constantly determined among them.

As can be seen from the foregoing, a number of virtual point light sources $Q_i(x_1, y_1, z_1)$ are located on a side opposite to the viewing side of three-dimensional object 10 that can be recorded and reconstructed as CHG 12. The luminance angle distribution $T_{WLCi}(\theta_{xz}, \theta_{yz})$ of light

divergent from each virtual point light source Q_i is set in such a way as to become equal to that on the surface of that three-dimensional object 10 as the virtual point light source Q_i is viewed from the viewing side through the three-dimensional object 10, and the initial phase ϕ_{wLci} of the virtual point light source Q_i is mutually independently and constantly set among virtual point light sources Q_i . Divergent light beams from such virtual point light sources Q_i are superimposed one upon another on the plane of CGH 12, and the ensuing superposed phase and amplitude are holographically recorded in a given position (by interference with reference light 2), thereby obtaining CGH 12 that can reconstruct the three-dimensional object 10.

15 In the arrangement of Fig. 1, it is noted that CGH 12 is not necessarily positioned on the viewing side of object 10; it could be located anywhere on the viewing side of virtual point light source group 11. It is also noted that the object 10 is not necessarily positioned on the viewing side of virtual point light source group 11.

20 As reconstructing illumination light 15 having the same wavelength λ_c as that of reference light 2 is entered in the thus fabricated CGH 12 at the same angle of incidence as that of reference light 2 as shown in Fig. 2, the object (three-dimensional object) 10 is reconstructed as a virtual image (often as a real image depending on the position of CGH 12 relative to object 10) by diffraction

light 16 diffracted from CGH 12, enabling viewer M to view that three-dimensional object 10. By movement of the point of view, the viewer will be capable of viewing the object 10 with satisfactory three-dimensional effects. It is here understood that although diffraction light 16 propagates as if it left virtual point light source group 11, yet that group 11 is hard to perceive directly because the light leaving each virtual point light source varies in luminance with directions.

How to fabricate such CGH 12 in the form of a binary hologram is now explained with reference to Fig. 3. At step ST1, the shape of the object 10 to be fabricated as a CGH is defined. Then, at step ST2, a spatial arrangement for a virtual point light source group 11, object 10, CGH 12 and reference light 2, a sampling point (Q_i) for virtual point light source group 11 and a sampling point (P_j) for CGH 12 are defined. Then, at step ST3, a luminance angle distribution T_{WLCi} (θ_{xz} , θ_{yz}) for each virtual point light source is set in such a way as to become equal to that on the surface of object 10. Then, at step ST4, the complex amplitude value O_{WLC} (x_2 , y_2 , z_2) of object light and the complex amplitude value R_{WLC} (x_2 , y_2 , z_2) of reference light 2 on the plane of CGH 12 are calculated from equations (1) and (2). Thereafter, at step ST5, the intensity of interference fringes of object light and reference light is found from equation (3) at each sampling point defined on the plane of CGH 12, so

that interference fringe data are obtained. Following this, the obtained interference fringe data are quantized at step ST6 and then converted into EB lithographic rectangular data at step ST7, which are finally recorded
5 in a medium on an EB lithography system, resulting in CGH 12.

While, in Fig. 1, object waves from all virtual point light sources Q_i are shown as being incident on the cell P_j of CGH 12, it is understood that the virtual point
10 light source group 11 and CGH 12 could be divided to a number of slice planes vertical to the y-axis in such a way that the range of incidence of waves could be limited to within the slice planes.

In Fig. 1, while point light sources in a two-
15 dimensional plane are used as the virtual point light sources, it is acceptable to employ line light sources emitting light that does not go as far as the y-direction.

In Fig. 1, the interference of object light and reference light is used so as to fix the complex amplitude
20 value $O_{wLc}(x_2, y_2, z_2)$ as a hologram. However, it is acceptable to rely upon Lohmann's method and Lee's method (Non-Patent Publication 1) for direct reconstruction of the complex amplitudes of object waves, and the method proposed by the inventors in Patent Publication 9 as well.

25 Fig. 4 is illustrative of another embodiment of the computer-generated hologram according to the invention, wherein the virtual point light source group 11 and CGH 12 of Fig. 1 are interchanged and the virtual point light

source group 11 is replaced by a virtual condensing point group 13. As shown in Fig. 4, CGH 12, an object 10, a virtual condensing point group 13 and a viewer M are located in this order in a + direction along a z-axis.

5 With the center of CGH 12 defining the origin of coordinates, x- and y-axes are determined in mutually orthogonal directions and in a direction orthogonal with respect to the z-axis. With the coordinates of the group of virtual condensing point group 13 described in terms of

10 (x_1, y_1, z_1) , the coordinates of object 10 in terms of (x_0, y_0, z_0) and the coordinates of CGH 12 in terms of (x_2, y_2, z_2) , the radiance of object 10 in θ_{xz} and θ_{yz} directions at a point S (x_0, y_0, z_0) that is observable from viewer M among the points of intersection of object 10 with a

15 straight line $Q_i P_j$ connecting an i-th virtual condensing point $Q_i (x_1, y_1, z_1)$ with a j-th cell $P_j (x_2, y_2, z_2)$ of CGH 12 is represented by $T_{WLCi} (\theta_{xz}, \theta_{yz})$. Here θ_{xz} is an angle of straight light $Q_i P_j$ with the z-axis upon projected onto an x-z plane, and θ_{yz} is an angle of

20 straight line $Q_i P_j$ with the z-axis upon projected onto a y-z plane.

Given that λ_c is a wavelength, ϕ_{WLCi} is the phase of wavelength λ_c of virtual condensing point Q_i , and r_{ij} is the Q_i to P_j distance. Then, the complex amplitude value

25 $O_{WLC} (x_2, y_2, z_2)$ of an object wave incident on $P_j (x_2, y_2, z_2)$ becomes, rather than the aforesaid equation (1),

M

$$O_{WLC}(x_2, y_2, z_2) = \sum_{i=1}^M \{ T_{WLCi}(\theta_{xz}, \theta_{yz}) / |r_{ij}| \} \times \exp[j\{-(2\pi/\lambda_c)|r_{ij}| + \phi_{WLCi}\}] \quad \dots (1')$$

Here the incident vector of reference light 2 incident on CGH 12 and consisting of parallel light is given by (R_x, R_y, R_z) , the amplitude of wavelength λ_c thereof by R_{WLC0} , and the phase thereof at the origin of the coordinates by ϕ_{RWLC} . Then, as is the case with Fig. 1, the complex amplitude value of reference light 2 becomes

$$R_{WLC}(x_2, y_2, z_2) = R_{WLC0} \cdot \exp[j\{2\pi/\lambda_c \times (R_x x_2 + R_y y_2 + R_z z_2) / (R_x^2 + R_y^2 + R_z^2)^{1/2} + \phi_{RWLC}\}] \quad \dots (2)$$

Likewise, the intensity value, $I_{WLC}(x_2, y_2, z_2)$, of interference fringes of object wave and reference light 2 at $P_j(x_2, y_2, z_2)$ becomes

$$I_{WLC}(x_2, y_2, z_2) = |O_{WLC}(x_2, y_2, z_2) + R_{WLC}(x_2, y_2, z_2)|^2 \quad \dots (3)$$

In the above equations, the Q_i to P_j distance r_{ij} is

$$r_{ij} = \{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2\}^{1/2} \quad \dots (4)$$

The angle θ_{xz} of straight line $Q_i P_j$ with the z-axis upon projected onto the x-z plane is

$$\theta_{xz} = \tan^{-1}\{(x_2 - x_1) / (z_2 - z_1)\} \quad \dots (5)$$

The angle θ_y of straight line $Q_i P_j$ with the z-axis upon projected onto the y-z plane is

$$\theta_{yz} = \tan^{-1}\{(y_2 - y_1) / (z_2 - z_1)\} \quad \dots (6)$$

The initial phase ϕ_{WLCi} of each virtual condensing point Q_i is mutually independently and constantly determined among virtual condensing points Q_j .

As can be seen from the foregoing, a number of
5 virtual condensing points Q_i (x_1, y_1, z_1) are located on the viewing side of three-dimensional object 10 that can be recorded and reconstructed as CGH 12. The luminance angle distribution T_{WLCi} (θ_{xz}, θ_{yz}) of convergent light incident from the object side on each virtual condensing
10 point Q_i is set in such a way as to become equal to that of the surface of that three-dimensional object 10 as the three-dimensional object 10 is viewed from the viewing side through the virtual condensing point Q_i , and the initial phase ϕ_{WLCi} at the virtual condensing point Q_i is
15 mutually independently and constantly set among virtual condensing points Q_i . Convergent light beams on such virtual condensing points Q_i are superimposed one upon another on the plane of CGH 12, and the ensuing superposed phase and amplitude are holographically recorded in a
20 given position (by interference with reference light 2), thereby obtaining CGH 12 that can reconstruct the three-dimensional object 10.

In the arrangement of Fig. 4, it is noted that CGH 12 is not necessarily located on the side opposite to the
25 viewing side of the object 10; it could be located anywhere on the side opposite to the viewing side of the virtual condensing point group 13. It is also noted that

the object 10 is not necessarily positioned on the side opposite to the viewing side of the virtual condensing point group 13.

It is noted the luminance angle distribution T_{WLci}
5 $(\theta_{xz}, \theta_{yz})$ of convergent light from the object side on the above virtual condensing point Q_i is the same as that for a computer graphic image generated with a computer graphic camera located at the position of virtual condensing point Q_i , as shown in Fig. 4, and so the calculation of equation
10 $(1')$ can be simplified because usable to this end is a computer graphic image (3D CG image) generated using commercial software with the point of view placed on the virtual condensing point Q_i .

As reconstructing illumination light 15 having the same wavelength λ_c as that of reference light 2 is entered in the thus fabricated CGH 12 at the same angle of incidence as that of reference light 2 as shown in Fig. 5, the object (three-dimensional object) 10 is reconstructed as a real image (often as a virtual image depending on
20 the position of CGH 12 relative to the object 10) by diffraction light 16 diffracted from CGH 12, enabling viewer M to view that three-dimensional object 10. By movement of the point of view, the viewer will be capable of viewing the object 10 with satisfactory three-
25 dimensional effects. It is here understood that although diffraction light 16 propagates as if it left the virtual condensing point group 13, yet the virtual condensing

point group 13 is hard to perceive directly because the light leaving each virtual condensing point varies in luminance with directions.

How to fabricate such CGH 12 as explained with reference to Figs. 4 and 5 in the form of a binary hologram is now explained with reference to Fig. 6. Fig. 6 is essentially similar to Fig. 3 with the exception that at step ST2, an arrangement of CGH 12, object 10, virtual condensing point group 13 and reference light 2, a sampling point (P_j) for CGH 12 and a sampling point (Q_i) for virtual condensing point group 13 are defined; at step ST3, the luminance angle distribution $T_{WLCi}(\theta_{xz}, \theta_{yz})$ for each virtual condensing point is set in such a way as to become equal to that on the surface of object 10; and at step ST4, the complex amplitude value $O_{WLC}(x_2, y_2, z_2)$ of object light and the complex amplitude value $R_{WLC}(x_2, y_2, z_2)$ of reference light 2 on the plane of CGH 12 are calculated from equations (1') and (2), and so no further explanation is made herein.

In this embodiment, too, object waves incident on all virtual condensing points Q_i are shown as being incident on the cell P_j of CGH 12, it is understood that the virtual condensing point group 13 and CGH 12 could be divided to a number of slice planes vertical to the y-axis in such a way that the range of incidence of waves could be limited to within the slice planes.

In Fig. 4, while point light sources in a two-

dimensional plane are used as the virtual condensing points, it is acceptable to employ line light sources emitting light that does not go as far as the y-direction.

In Fig. 4, the interference of object light and
5 reference light is used so as to fix the complex amplitude value $O_{WLC}(x_2, y_2, z_2)$ as a hologram. However, it is acceptable to rely upon Lohmann's method and Lee's method (Non-Patent Publication 1) for direct reconstruction of the complex amplitudes of object waves, and the method
10 proposed by the inventors in Patent Publication 9 as well.

The CGH 12 according to the invention has been described with reference to how to generate a stereoscopic image on the basis of the three-dimensionally shaped (3D CG) object 10 to be recorded; however, the invention is
15 not limited thereto. For instance, if an image obtained by taking an image of a real object using a camera with a lens located at each virtual condensing point Q_i and digitalizing that image, rather than a computer graphic image, is used as the distribution $T_{WLCi}(\theta_{xz}, \theta_{yz})$ in the
20 arrangement of Fig. 4, it is then possible to achieve a computer-generated hologram capable of reconstructing a stereoscopic image of that real image.

As an image is generated by gradual movement of a stereoscopic object for each variation of the position of
25 virtual condensing points Q_i (i.e., the position of a camera), it is possible to obtain an additional animation effect that enables a stereoscopic image to be viewed as

if a stereoscopic image moved gradually with a variation in viewing position. This may be applied to the use of a computer graphic image or the case where an image of a real object is taken.

5 While this may also be applied to a conventional one-step holographic stereogram, it is understood that with the computer-generated hologram of the invention, it is possible to obtain ever higher resolution, because the CGH plane is so separated from the position of the group
10 of virtual point light sources or virtual condensing points that the density of virtual point light sources or virtual condensing points can be increased, creating a reconstructed image having no distortion and improved quality.

15 While the computer-generated hologram of the invention has been described with reference to its principles, it should be understood that the invention is in no sense limited to the embodiments described so far and so many other modifications may be made.

20 In accordance with the computer-generated hologram of the invention, the position of condensing reconstruction light diffracted from the hologram is separated from the object to be reconstructed and the hologram plane. It is thus possible to achieve a
25 computer-generated hologram that has no pixel structure on the hologram plane with much more parallaxes and ever higher resolution, creating a reconstructed image having no image distortion problem and much higher quality. It

is also possible to provide a computer-generated hologram that makes any holographic photostep unnecessary, ensures simplified image processing, and makes a computer graphic image of a three-dimensional object obtained on commercial
5 software available as the stereoscopic image to be recorded.